

Conserved charge fluctuations are not conserved during the hadronic phase

J. Steinheimer¹, V. Vovchenko^{1,2,3}, J. Aichelin^{1,4}, M. Bleicher^{1,2}, and H. Stöcker^{1,2,5}

¹ *Frankfurt Institute for Advanced Studies, Ruth-Moufang-Str. 1, 60438 Frankfurt am Main, Germany*

² *Institut für Theoretische Physik, Goethe Universität Frankfurt,
Max-von-Laue-Strasse 1, D-60438 Frankfurt am Main, Germany*

³ *Department of Physics, Taras Shevchenko National University of Kiev, 03022 Kiev, Ukraine*

⁴ *SUBATECH, UMR 6457, Université de Nantes, Ecole des Mines de Nantes,
IN2P3/CNRS, 4 rue Alfred Kastler, 44307 Nantes cedex 3, France and*

⁵ *GSI Helmholtzzentrum für Schwerionenforschung GmbH, D-64291 Darmstadt, Germany*

We study the correlation between the distributions of the net-charge, net-kaon, net-baryon and net-proton number at hadronization and after the final hadronic decoupling by simulating ultra relativistic heavy ion collisions with the hybrid version of the ultrarelativistic quantum molecular dynamics (UrQMD) model. We find that due to the hadronic rescattering these distributions are not strongly correlated. The calculated change of the correlation, during the hadronic expansion stage, does not support the recent paradigm, namely that the measured final moments of the experimentally observed distributions do give directly the values of those distributions at earlier times, when the system had been closer to the QCD crossover.

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In this letter we will question whether the fluctuations observed in high energy nuclear collisions can be related to the fluctuations close to the QCD pseudo critical line from lattice gauge calculations, an idea which has been recently advanced by several authors [1–4].

The collision of heavy ions at relativistic energies allows for the creation of ultra dense baryonic matter at very high energy densities and temperatures. It is expected from quantum chromodynamics (QCD) that matter undergoes a transition to a novel state of matter called the quark-gluon-plasma (QGP) [5] at high temperatures and even into a quarkyonic [6] or a color-flavor-locked phase [7] at high baryon densities and moderate temperatures. Event-by-event fluctuations of conserved charges, measured in relativistic nuclear collisions, moved recently in the center of attention in the search of a possible first order phase transition and critical endpoint in the phase diagram of QCD [8, 9]. Higher order cumulants of the net-charge distributions (related to the susceptibilities) are sensitive probes of the underlying equation of state and hence of the phase structure. However, they are also very sensitive to other effects which are not related to the underlying physics of interest. Such effects include the correct understanding of efficiency and acceptance effects in experimental setups [10–12], influences from cluster formation [14], influence of conservation laws [15, 16], corrections due to the finite size of the system created in relativistic nuclear collisions [17], and fluctuations of the system volume [18, 19]. Experiments have reported on measurements of conserved charge fluctuations (see e.g. [20–22]), but up to date most studies compare the cumulants computed on the lattice or within grand canonical effective models such as the hadron resonance gas (HRG) model, directly to the experimental data [23–25]. It is important to note that in fact exper-

iments can measure directly only the net-electric charge distribution and, thus, one relies on measurements of the net-proton and net-kaon distributions as proxies for the net-baryon and net-strangeness distributions [13]. Several studies have suggested that in fact the elastic and inelastic scattering in the hadronic phase, which follows the hadronization process in nuclear collisions, may have a significant impact on the observed cumulants [26–28], and may further blur the correlation of particle number fluctuations and net-charge fluctuations. Quantitative statements are, however, difficult as they require a microscopic transport treatment of the hadronic rescattering phase (see e.g. [29]).

We will show in this letter that hadronic rescattering, based on known reaction cross sections, decorrelates strongly the distributions of conserved charges between hadronization and kinetic freeze-out. Thus the experimentally observed moments of this distribution are only weakly correlated with the moments of the distribution at hadronization, i.e. at the boundary between the QGP and the hadronic world.

THE MODEL

For our investigations we will utilize the newest version of the UrQMD hybrid model [30], which employs the UrQMD hadronic transport model to simulate the non-equilibrium initial and final phases of the nuclear reactions, where the bulk evolution of the hot and dense phase is simulated by a 3+1 dimensional ideal fluid dynamics code. The fluid dynamical equations for conservation of energy-momentum as well as the conservation of the net-baryon number current are solved by the SHASTA algorithm [31]. The transition from the initial non-equilibrium phase to the fluid dynamical evolution is

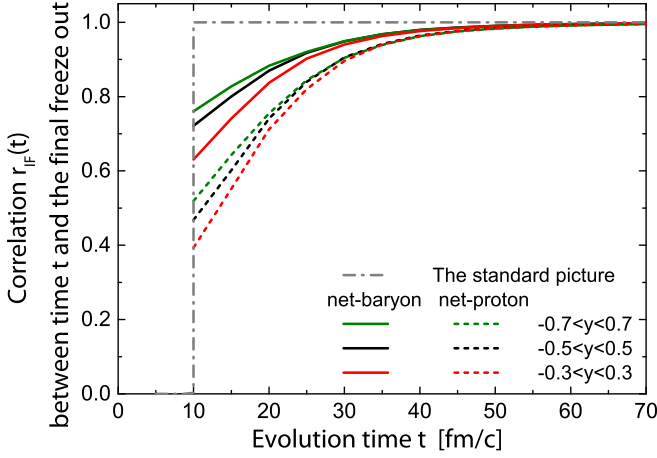


FIG. 1. [Color online] Correlation of the finally observed net-charge, net-kaon, net-proton and net-baryon number in different rapidity intervals with an earlier time t in that same rapidity interval. Results for central collisions of Au+Au at a beam energy of $\sqrt{s_{NN}} = 200$ GeV are shown.

done at a time t_{INI} defined as the interpenetration time, the earliest instant at which local equilibration can be achieved (with the constraint that $t_{INI} \geq 0.5$ fm/c).

$$t_{INI} = \frac{2R}{\gamma_{CM} v} = \frac{2R}{\sqrt{\gamma_{CM}^2 - 1}} \quad (1)$$

where R is the radius of the nucleus and γ_{CM} is the Lorentz gamma factor of the two nuclei in their center of mass frame. The transition back to discrete particles from the fluid dynamical fields is done in the standard fashion, by employing the Cooper-Frye prescription [32] on a pre-defined hypersurface. In this work we will employ the iso-energy density hypersurface [33] of $e_{CF} \approx 350$ MeV/fm³. To ensure global energy conservation as well as conservation of the different net-charges (electric, baryon number and strangeness) we also use a rejection method during the Monte-Carlo sampling of the Cooper-Frye equation (eq. (2)). Hadrons which have been produced at the hypersurface interact during the hadronic rescattering phase in the UrQMD model [34, 35]. To describe this stage we use the cascade version of the code, where all interactions between hadrons are determined by a geometric criterion tied to their specific scattering cross section. The model includes close to 60 different baryonic species and their anti-particles as well as about 40 mesonic states.

The corresponding momentum dependent scattering cross sections are taken from experiment where known and from the additive quark model otherwise. The reactions implemented in the model include elastic $2 \leftrightarrow 2$ scatterings as well as inelastic reactions like resonance excitations and decays, strangeness exchange and annihilation reactions. A detailed analysis of the reactions in

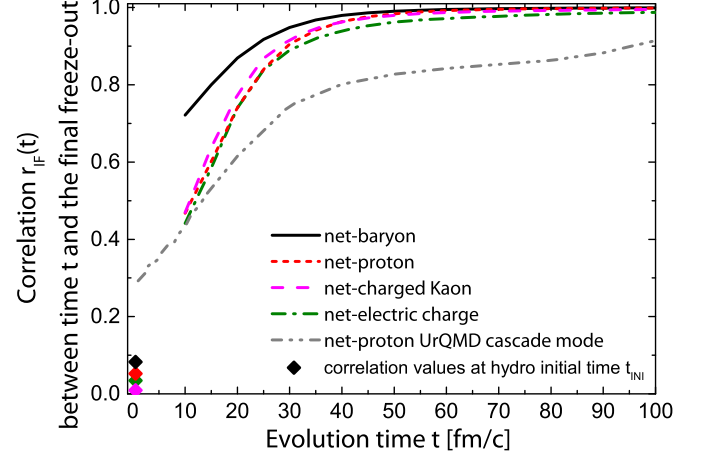


FIG. 2. [Color online] Correlation of the net-charge, net-kaon, net-proton and net-baryon number in the rapidity interval $-0.5 < y < 0.5$ with an earlier time t in that same rapidity interval.

the final hadronic stage of an ultra relativistic heavy ion collision can be found in [36].

As we intend to study the effects of the hadronic rescattering on fluctuation measures as the cumulants of the different net-charge distributions, we first have to discuss some specific relevant difficulties associated with the current state-of-the-art fluid dynamical models. In the usual framework of fluid dynamical models, as well as of the hybrid models such as the one employed in this study, the transition from the fluid dynamical fields to a finite and discrete number of particles is done by a Monte-Carlo sampling of the Cooper-Frye equation on a specific hypersurface σ_μ

$$E \frac{dN}{d^3p} = \int_\sigma f(x, p) p^\mu d\sigma_\mu. \quad (2)$$

It is important to note that the single particle distribution functions $f(x, p)$ which enter the Cooper-Frye formula are usually assumed to be the grand canonical Fermi or Bose distributions for a hadron resonance gas at a given temperature T and chemical potential μ_i . These single-particle distribution functions are generally uncorrelated, as expected for a non-interacting HRG, and, since the particle number in a given local computational cell is much smaller than 1, the particle number distributions locally follow the Poisson distribution. It is therefore obvious that, using this standard method of particlization, one cannot obtain a net-charge distribution which is different from a Poisson distribution except for effects stemming from the global conservation of net-charges, as enforced by the particle production scheme employed in the UrQMD-hybrid model. Thus, the comparison of the (normalized) cumulants before and after the hadronic rescattering phase will not lead to new in-

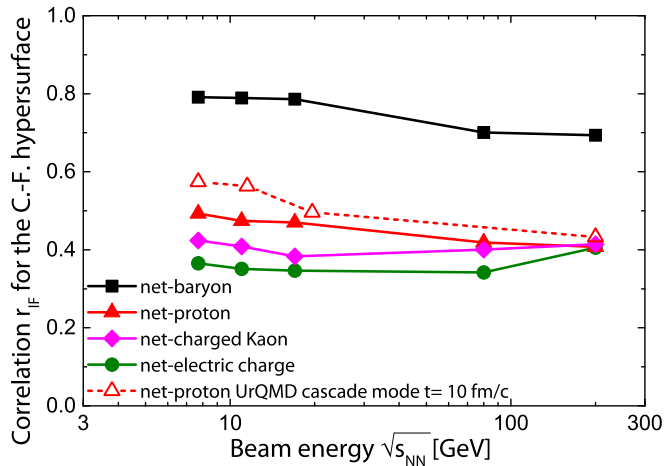


FIG. 3. [Color online] Correlation of the finally observed net-charge, net-kaon, net-proton and net-baryon number in the rapidity interval $-0.5 < y < 0.5$, at the Cooper-Frye hypersurface, with the final net-charge density as a function of beam energy.

sights as in this case one starts with a Poisson distribution.

In the current paper we will take a different approach to make qualitative and quantitative statements. We will set-up a time-dependent correlation function to explore the diffusion of conserved charges during the hadronic phase. Following the standard definition of the correlation coefficient this function reads as

$$r_{\text{IF}}(t) = \frac{\sum_n (I_n(t) - \bar{I}(t))(F_n - \bar{F})}{\sqrt{\sum_n (I_n(t) - \bar{I}(t))^2 \sum_n (F_n - \bar{F})^2}}, \quad (3)$$

where $I_n(t)$ denotes the number of a given charge (or a net-particle number) in a given rapidity and momentum window at the time t in the event number n . F_n is the final number of that charge after all interactions have ceased, in the same event. Finally, the $\bar{I}(t)$ and \bar{F} are the corresponding averages. The sum runs over all events in the sample. It is evident that if the net-charge in a given bin at a given time t is perfectly correlated with the net-charge at the end of the evolution, then the value of this correlation function $r_{\text{IF}}(t)$ will be equal to 1 whereas if the net-charge number at given time t is completely uncorrelated with the final value, then the $r_{\text{IF}}(t)$ will be equal to zero.

In the standard scenario [4], which is employed in most comparisons of the (normalized) cumulants with the HRG or lattice QCD results one essentially assumes that this correlation is equal to zero before the chemical freeze-out of hadrons and then instantly jumps to one at the chemical freeze-out, a value which does not change until the cumulants are observed by experiment. This scenario is shown in figure 1 by a grey dash dotted line for

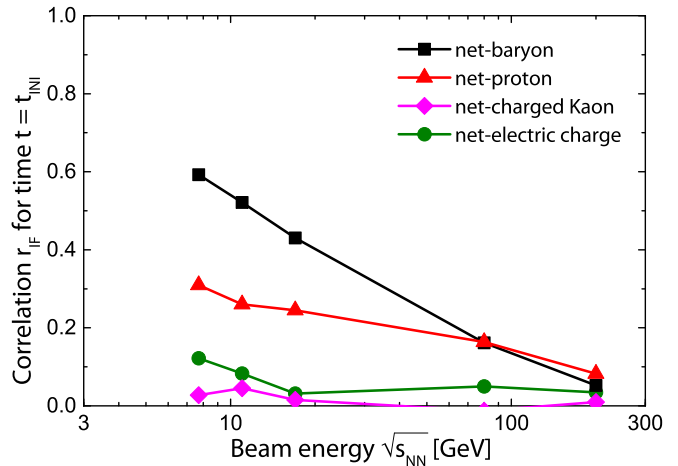


FIG. 4. [Color online] Correlation of the net-charge, net-kaon, net-proton and net-baryon number in the rapidity intervals $-0.5 < y < 0.5$ at the initial hydro time with the final net-charge density in that same rapidity interval, as a function of beam energy.

an exemplary freeze-out time of 10 fm/c. In such a scenario the final value of the cumulants correspond to that at chemical freeze-out, without any information about the QGP phase before freeze-out or about the hadronic rescattering which follows hadronization.

RESULTS

We start by studying the correlation of different net-charges in central ($b < 3.4$ fm) collisions of gold nuclei at beam energy of $\sqrt{s_{\text{NN}}} = 200$ GeV, as measured at the Relativistic Heavy Ion Collider (RHIC) at the Brookhaven National Laboratory (BNL). We will investigate the correlation of the net-electric charge, the net-kaon number, the net-baryon number and the net proton number within our model. For the net-proton and net-baryon number we also apply a cut in transverse momentum of $0.3 < p_T < 2.0$ GeV, which corresponds approximately to the relevant experimental acceptance window. All these quantities, except the net-baryon number which is inaccessible with the current detectors, have been studied in experiments at the RHIC.

To estimate the effect of the full local equilibration on the decorrelation of the different charges we will also contrast the hybrid model simulations with results obtained from the standard UrQMD model in its cascade version. In the cascade version of the model, the system remains essentially out of local equilibrium for a long time and, due to the finite cross sections, will retain more information and therefore show a stronger correlation with the early times.

First we focus on the influence of the size of the rapidity acceptance window. Figure 1 depicts the correlation of

the net-baryon number and net-proton number as a function of time for central Au+Au reactions at $\sqrt{s_{NN}} = 200$ GeV. We present the correlation for times $t > 10$ fm/c as the net-proton number cannot be defined during the deconfined phase which dominates the dynamics at earlier times. A dependence on the size of the rapidity window is clearly present. As expected, a larger acceptance window leads to a stronger correlation of the initial and final net-charge number in a single event. We also observe a stronger correlation of the net-baryon number with the finally observed number than for the net-proton number, which is also expected, as protons can easily exchange isospin and become neutrons during the rescattering phase, e.g. through the excitation and decay of a Δ resonance.

Figure 2 shows the dependence of the correlation $r_{IF}(t)$, for different net-charge and net-particle numbers, as a function of time. Unlike in the standard scenario assuming instant freeze-out, the correlation function strongly depends on the duration of the rescattering phase for all considered quantities. At very late times ($t > 40$ fm/c) the correlation function approaches 1, which is expected as the system has essentially frozen out and interactions have ceased by that time. However, the correlation changes rapidly in the time interval between particle production (on the Cooper-Frye hypersurface) at around 10 fm/c and decoupling of the system at about 25 fm/c. At the time of interest for most studies, namely the particle production time, the correlation is approximately 0.5 for most net-charges. Only the net-baryon number correlation is slightly stronger, as discussed above. However, the quantity that is measured experimentally, namely the net-proton number, shows a similar correlation as the net-charge, as significant isospin changing reactions take place during the rescattering phase. The net protons in the case of the full cascade UrQMD simulation show a larger initial correlation and an even slower increase of the correlation function compared to the hybrid simulation, hinting to a smaller number of scatterings in the early high density phase and an extended emission period. This is likely due to the smaller radial flow in the cascade simulation due to the lack of scatterings in the early stage of the collision.

There are two crucial points in time at which we want to study the correlation $r_{IF}(t)$ in more detail. One is the time at which hadrons are produced according to chemical equilibrium distributions. At this point, at the transition between the hadronic and quark phase, the hadrons are sampled from the transition (hadronization) hypersurface according to the Cooper-Frye equation. The second one is an even earlier time at which the fluid dynamical evolution starts. The second point is of interest because one can identify possible correlations which survive the fluid dynamical evolution. This can be, for example, correlations which stem from the initial stopping of the participant nucleons and which may have an influence on the final net-charge distributions. Therefore

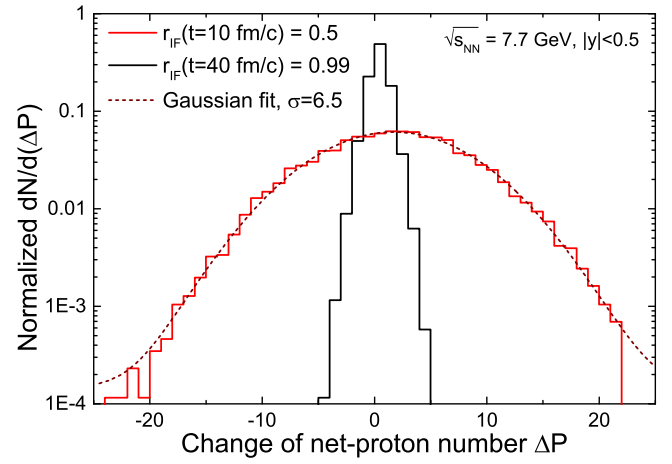


FIG. 5. [Color online] Probability distribution of the change of the net-proton number in the time interval between $t = 10$ fm/c (red line), $t = 40$ fm/c (black line) and the last scattering. We show results for $\sqrt{s_{NN}} = 7.7$ GeV. The corresponding correlation values $r_{IF}(t)$ are 0.5 for $t = 10$ and 0.99 for $t = 40$ fm/c. We also fitted the distribution for $t = 10$ fm/c with a Gaussian function and obtained a width $\sigma = 6.5$ which is close to the width of the final net-proton distribution $\sigma_{final} = 7.5$.

we show in figure 3 the correlation $r_{IF}(t = t_{CF})$ which is defined as the correlation between the net-particle number going through the Cooper-Frye hypersurface and the final state particle number. This correlation apparently shows only a very weak beam energy dependence down to $\sqrt{s_{NN}} = 7$ GeV. This means that the importance of the hadronic rescattering does not change much within the beam energy range of the beam energy scan program at RHIC. The results from the standard cascade UrQMD simulations show a similar correlation for all considered beam energies at $t = 10$ fm/c.

More important the beam energy dependence of the correlation $r_{IF}(t = t_{INI})$, defined as the correlation between the net-particle number at the starting time of the fluid dynamical simulation and the final particle number, shows a clear energy dependence in figure 4. It increases with decreasing beam energy. While at the top RHIC energy, essentially no information on baryon stopping survives the fluid dynamical phase, at low energies the conservation of the stopped baryon number throughout the fluid dynamical evolution generates a significant correlation.

As a last step we will demonstrate the effect of the decorrelation of the different net-charge and net-particle numbers on their final number distributions. To do so we look at the distribution of the change of a particular net-particle number (i.e. the net-proton number) for different values of $r_{IF}(t)$ as extracted from our simulations. The change of the net-proton number ΔP is defined as the final net-proton number in a single event minus the net-proton number at a given time t in that single event.

If at time t the event has already its final net-proton number we find, $r_{\text{IF}}(t) = 1$, and the distribution of ΔP would be a delta function with a possible shift along the ΔP -axis. The smaller the value of $r_{\text{IF}}(t)$ becomes, the broader we expect the distribution of the change to be. Figure 5 shows this distribution function for two different values of $r_{\text{IF}}(t)$, at times $t = 10$ fm/c and $t = 40$ fm/c, for central collisions at a beam energy of $\sqrt{s_{\text{NN}}} = 7.7$ GeV. We observe that already for a small decorrelation $r_{\text{IF}}(t = 40) = 0.99$, we obtain a distribution which does not closely resemble a delta function but rather a Gaussian with finite width, even though the width is very small compared to the mean net-proton number which is 46. However, for a correlation of $r_{\text{IF}}(t = 10) = 0.5$, the change of the net-proton number has a broad distribution. We were able to fit this distribution with a Gaussian of width $\sigma = 6.5$, which is only slightly smaller than the width of the final net-proton number distribution which is 7.5. Note that one may use detailed information on the smearing from model studies such as ours, to try to reconstruct the initial cumulants near hadronization.

SUMMARY

We have explored the time dependence of the correlation function of conserved charges in Au+Au reactions at various beam energies. We found that the hadronic rescattering phase leads to a substantial decorrelation of the conserved charge distributions. This effect is present for all investigated conserved charges and is mostly energy independent. This means that the final distribution function, the only one which can be observed, is to a large extent uncorrelated to that of the newly born hadrons which may carry information on the quark phase of QCD. Hence, a naive comparison of the experimentally measured correlations with the values as calculated by lattice QCD, appropriate for a stationary and infinite model system only, can produce unjustified and misleading conclusions on the phase structure of QCD.

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[1] S. Ejiri, F. Karsch and K. Redlich, Phys. Lett. B **633**, 275 (2006).

[2] B. Friman, F. Karsch, K. Redlich and V. Skokov, Eur. Phys. J. C **71**, 1694 (2011).

[3] P. Braun-Munzinger, B. Friman, F. Karsch, K. Redlich and V. Skokov, Phys. Rev. C **84**, 064911 (2011).

[4] F. Karsch and K. Redlich, Phys. Lett. B **695**, 136 (2011).

[5] M. A. Stephanov, K. Rajagopal and E. V. Shuryak, Phys. Rev. Lett. **81**, 4816 (1998).

[6] L. McLerran and R. D. Pisarski, Nucl. Phys. A **796**, 83 (2007).

[7] M. G. Alford, A. Schmitt, K. Rajagopal and T. Schäfer, Rev. Mod. Phys. **80**, 1455 (2008).

[8] M. A. Stephanov, Phys. Rev. Lett. **102**, 032301 (2009).

[9] V. Koch, arXiv:0810.2520 [nucl-th].

[10] A. Bzdak and V. Koch, Phys. Rev. C **86**, 044904 (2012).

[11] A. Bzdak, R. Holzmann and V. Koch, arXiv:1603.09057 [nucl-th].

[12] M. Kitazawa, Phys. Rev. C **93**, 044911 (2016).

[13] J. Noronha-Hostler, R. Bellwied, J. Gunther, P. Parotto, A. Pasztor, I. P. Vazquez and C. Ratti, arXiv:1607.02527 [hep-ph].

[14] Z. Fecková, J. Steinheimer, B. Tomášik and M. Bleicher, Phys. Rev. C **92**, no. 6, 064908 (2015).

[15] V. V. Begun, M. Gazdzicki, M. I. Gorenstein and O. S. Zozulya, Phys. Rev. C **70**, 034901 (2004).

[16] A. Bzdak, V. Koch and V. Skokov, Phys. Rev. C **87**, 014901 (2013).

[17] M. I. Gorenstein, M. Hauer, V. P. Konchakovski and E. L. Bratkovskaya, Phys. Rev. C **79**, 024907 (2009).

[18] M. I. Gorenstein and M. Gazdzicki, Phys. Rev. C **84**, 014904 (2011).

[19] E. Sangaline, arXiv:1505.00261 [nucl-th].

[20] N. Xu [STAR Collaboration], Nucl. Phys. A **931**, 1 (2014).

[21] L. Adamczyk *et al.* [STAR Collaboration], Phys. Rev. Lett. **113**, 092301 (2014).

[22] L. Adamczyk *et al.* [STAR Collaboration], Phys. Rev. Lett. **112**, 032302 (2014).

[23] S. Borsanyi, Z. Fodor, S. D. Katz, S. Krieg, C. Ratti and K. K. Szabo, Phys. Rev. Lett. **113**, 052301 (2014).

[24] H. T. Ding, F. Karsch and S. Mukherjee, Int. J. Mod. Phys. E **24**, 1530007 (2015).

[25] P. Alba, W. Alberico, R. Bellwied, M. Bluhm, V. Mantovani Sarti, M. Nahrgang and C. Ratti, Phys. Lett. B **738**, 305 (2014).

[26] M. Kitazawa and M. Asakawa, Phys. Rev. C **86**, 024904 (2012) [Erratum-ibid. C **86**, 069902 (2012)].

[27] M. Asakawa, U. W. Heinz and B. Muller, Phys. Rev. Lett. **85**, 2072 (2000).

[28] S. Jeon and V. Koch, Phys. Rev. Lett. **85**, 2076 (2000).

[29] V. P. Konchakovski, S. Haussler, M. I. Gorenstein, E. L. Bratkovskaya, M. Bleicher and H. Stoecker, Phys. Rev. C **73**, 034902 (2006).

[30] H. Petersen, J. Steinheimer, G. Burau, M. Bleicher and H. Stoecker, Phys. Rev. C **78**, 044901 (2008).

[31] D. H. Rischke, S. Bernard and J. A. Maruhn, Nucl. Phys. A **595**, 346 (1995).

[32] F. Cooper and G. Frye, Phys. Rev. D **10**, 186 (1974).

[33] P. Huovinen and H. Petersen, Eur. Phys. J. A **48**, 171 (2012).

[34] S. A. Bass *et al.*, Prog. Part. Nucl. Phys. **41**, 255 (1998) [Prog. Part. Nucl. Phys. **41**, 225 (1998)].

[35] M. Bleicher *et al.*, J. Phys. **G25**, 1859 (1999).

[36] In preparation.